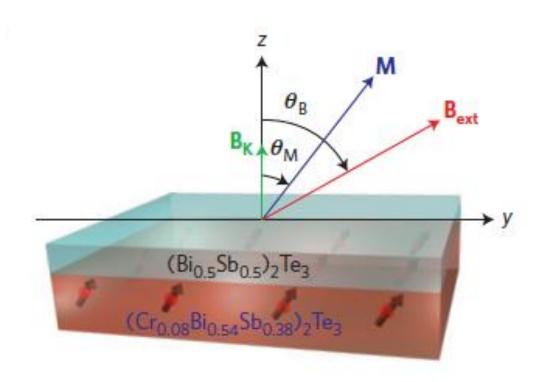
Topological Spintronic Devices

Current-Induced Torques & Topological Insulators

Massoud Masir, Nobu Okuma, Allan MacDonald UT Austin – SHINES collaboration



Spin-Orbit Torques in TI DMSs



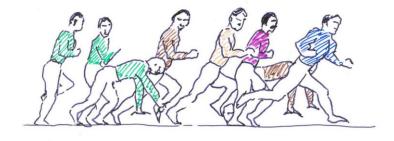
Fan et al., Nature Mat. (2014) Ndiaye et al. arXiv:1509.06929 Franz and Garate, PRL (2010) Theory of
 Current-Induced Torques

- Resistive Detection of SOTs
 - The role of the bulk?

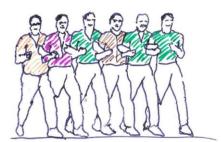
Emergent Collective DOF

Ferromagnet Heavy Metal

Incoherent motion

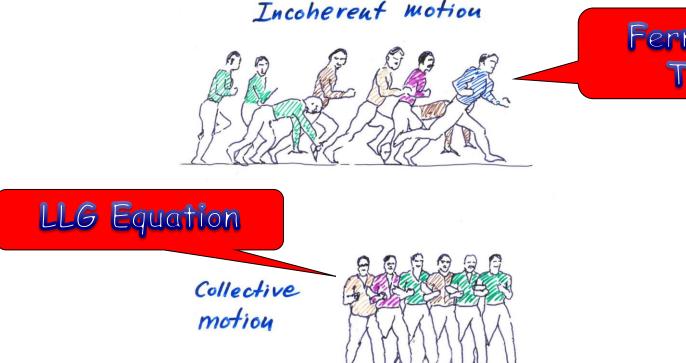


Collective motion



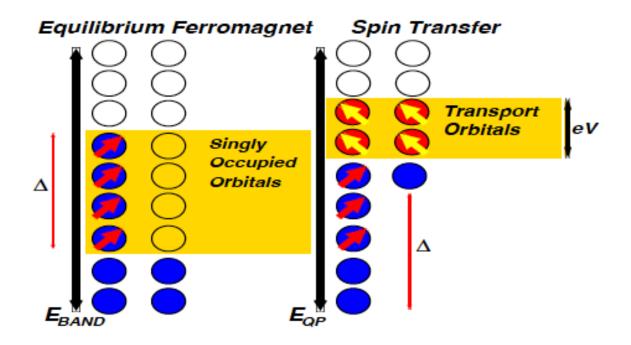
Emergent Collective DOF

Ferromagnet
Heavy Metal



Fermi Liquid
Theory

Spin-Torques Beyond Spin-Transfer

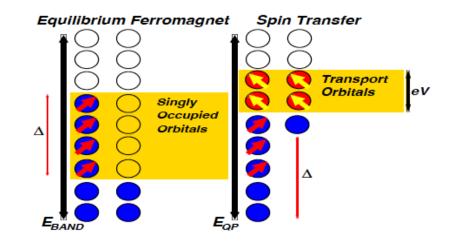


Alvaro Nunez - Ph.D. Thesis (2004) SSC (2006)

Spin-Torques Beyond Spin-Transfer

$$\delta \vec{H}_{eff} = \Delta(\vec{r}) \, \vec{m}_{\perp}$$

$$\vec{T} = (\hat{m} \times \vec{m}_{\perp}) \cdot \int d\vec{r} \, m(\vec{r}) \, \Delta(\vec{r})$$



Alvaro Nunez - Ph.D. Thesis (2004) 55C (2006) I. Garate PRB (2009)

Bulk Transport Theory Relaxation Time Approx

$$\frac{\partial \rho}{\partial t} = -\frac{i}{\hbar} \left[H, \ \rho \right] + \frac{1}{\hbar} \frac{\partial \rho}{\partial \mathbf{k}} \cdot e \mathbf{E} - \frac{\rho - \rho_0}{\tau}$$

Relaxation
Time
Approximation

Bulk Transport Theory

$$\frac{\partial \rho^{(0)}}{\partial \mathbf{k}} = \sum_{m} \left\{ \frac{\partial f_{m\mathbf{k}}}{\partial \mathbf{k}} |mk\rangle \langle mk| + f_{m\mathbf{k}} \left| \frac{\partial}{\partial \mathbf{k}} mk \right\rangle \langle mk| + f_{m\mathbf{k}} |mk\rangle \left\langle \frac{\partial}{\partial \mathbf{k}} mk \right| \right\}$$

$$[H,\;\rho]_{nn'}=\left(\varepsilon_{nk}-\varepsilon_{n'k}\right)\rho_{nn'}$$
 Off diagonal response is intrinsic when bands are well

Off diagonal defined

$$\left| \frac{\partial}{\partial \mathbf{k}} \, nk \right\rangle = \sum_{m \neq n} \left(\frac{\langle mk | \frac{\partial H}{\partial \mathbf{k}} | nk \rangle}{\varepsilon_{nk} - \varepsilon_{mk}} \right) | mk \rangle$$

Normal Transport Born Approximation

$$J_d(\langle \rho_{Ed} \rangle)_{m{k}} = D_{dm{k}}$$

$$D_{d\mathbf{k}} = \frac{e\mathbf{E}}{\hbar} \cdot \frac{\partial \langle \rho_{0\mathbf{k}}^n \rangle}{\partial \varepsilon_{n\mathbf{k}}}$$

$$J_d(\langle \rho_d \rangle)_{\mathbf{k}}^{nn} = \frac{2\pi}{\hbar} \sum_{n'\mathbf{k}'} \langle U_{\mathbf{k}\mathbf{k}'}^{nn'} U_{\mathbf{k}'\mathbf{k}}^{n'n} \rangle \left(\langle \rho_d \rangle_{\mathbf{k}}^n - \langle \rho_d \rangle_{\mathbf{k}'}^{n'} \right) \delta(\varepsilon_{\mathbf{k}}^n - \varepsilon_{\mathbf{k}'}^{n'})$$

Anomalous Transport Born Approximation

$$\frac{i}{\hbar} \left[H_{0\mathbf{k}}, \langle \rho_{Eod} \rangle_{\mathbf{k}} \right] = D_{od\mathbf{k}} - J_{od}(\langle \rho_{Ed} \rangle)_{\mathbf{k}}$$

$$D_{odk}^{nn'} \equiv \frac{eE}{\hbar} \cdot \langle u_{k}^{n} | \frac{\partial u_{k}^{n'}}{\partial k} \rangle (\langle \rho_{0} \rangle_{k}^{n} - \langle \rho_{0} \rangle_{k}^{n'})$$

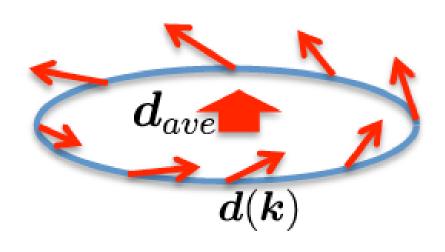
$$D'_{odk} = \frac{eE\tau_{p}\pi}{\hbar} \cdot \sum_{n'k'} \langle U_{kk'}^{nn'} U_{k'k}^{n'n''} \rangle \{ [v_{k}^{n}\delta(\varepsilon_{k}^{n} - \varepsilon_{F}) - v_{k'}^{n'}\delta(\varepsilon_{k'}^{n'} - \varepsilon_{F})] \delta(\varepsilon_{k}^{n} - \varepsilon_{k'}^{n'}) + [v_{k}^{n''}\delta(\varepsilon_{k'}^{n''} - \varepsilon_{F}) - v_{k'}^{n'}\delta(\varepsilon_{k'}^{n'} - \varepsilon_{F})] \delta(\varepsilon_{k'}^{n''} - \varepsilon_{F}) \}.$$

Theory of Current-Induced Torques

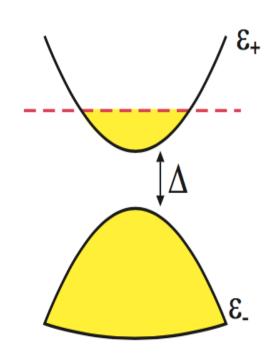
Resistive Detection of SOTs in TIs

The role of the bulk?

Massive Dirac Model for Current-Induced Spin Density



$$2v_D\delta\mathbf{s_k}\times\mathbf{b_k} + \frac{\delta\mathbf{s_k}}{\tau} = -\mathbf{F_k}$$



$$\mathbf{F}_{\mathbf{k}} = \left(\sum_{n} \langle n, \mathbf{k} | \mathbf{s} | n, \mathbf{k} \rangle \frac{\partial f_{n, \mathbf{k}}}{\partial \mathbf{k}} + \sum_{n} \sum_{m \neq n} \langle n, \mathbf{k} | \mathbf{s} | m, \mathbf{k} \rangle \left(\frac{f_{n, \mathbf{k}} - f_{m, \mathbf{k}}}{\varepsilon_{n, \mathbf{k}} - \varepsilon_{m, \mathbf{k}}} \right) \langle m, \mathbf{k} | \frac{\partial H}{\partial \mathbf{k}} | n, \mathbf{k} \rangle \right) \cdot \frac{e \mathbf{E}}{\hbar}$$

Magneto-resistance of Massive Dirac Model

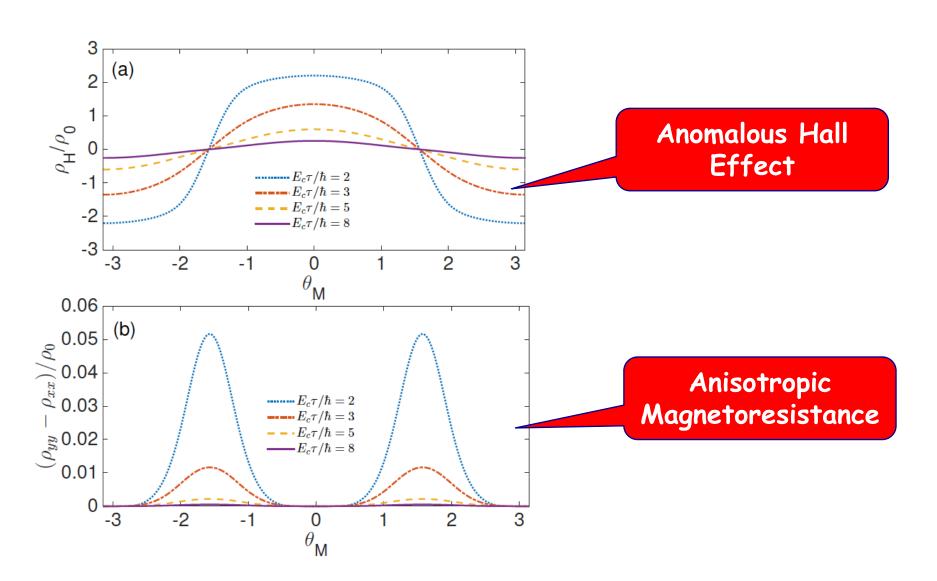
Anomalous Hall
Effect

$$\boldsymbol{\rho} = \begin{bmatrix} \rho_{\perp} \cos^{2} \varphi_{M} + \rho_{\parallel} \sin^{2} \varphi_{M} & \rho_{P} \cos \varphi_{M} \sin \varphi_{M} + \rho_{H} \\ \rho_{P} \cos \varphi \sin \varphi_{M} - \rho_{H} & \rho_{\perp} \sin^{2} \varphi_{M} + \rho_{\parallel} \cos^{2} \varphi_{M} \end{bmatrix}$$

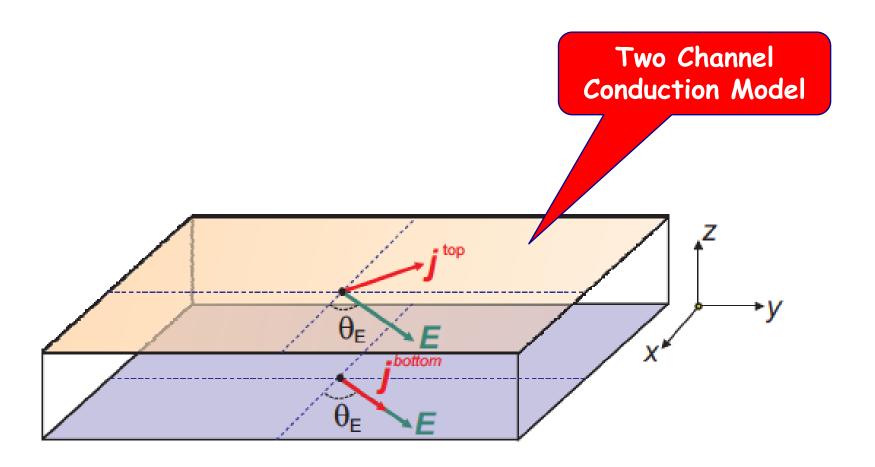
Anisotropic Magnetoresistance

$$\rho_P = \rho_{\parallel} - \rho_{\perp}$$

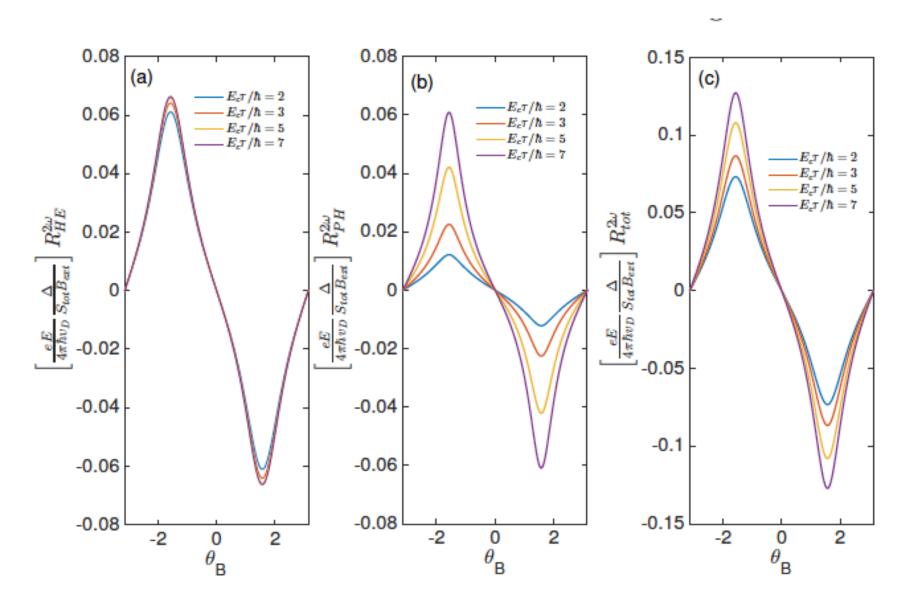
Magneto-resistance of Massive Dirac Model



Resistively Detected SOT



Resistively Detected SOT

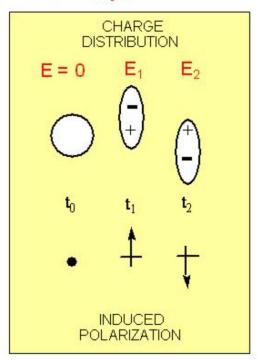


Theory of Current-Induced Torques: The case of TI DMSs

- Resistive Detection of SOTs
 - The role of the bulk?

Response of Atom to Static Electric Field

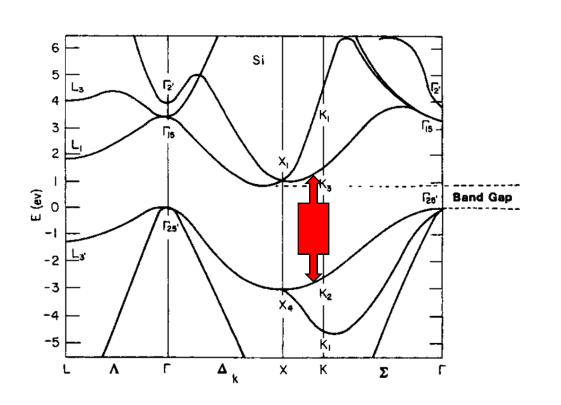
$$F = qE$$



$$\Psi_n^{(1)} = \sum_{k \neq n} \Psi_k^{(0)} \frac{V_{kn}}{E_n^{(0)} - E_k^{(0)}}$$

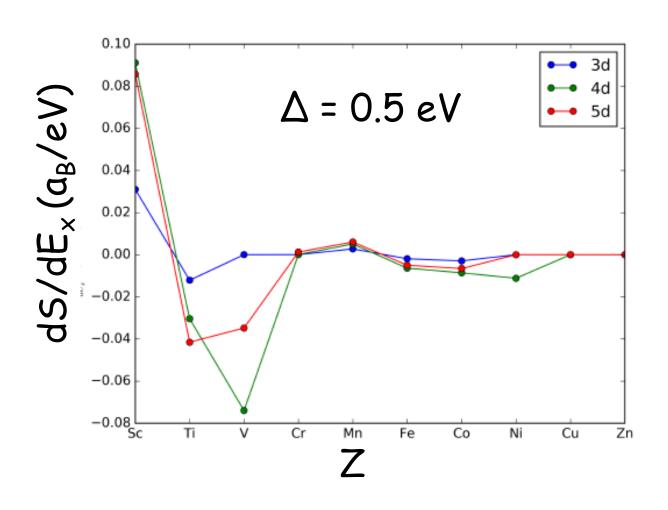
$$\alpha = e^2 \sum_{k \neq n} \frac{\mathbf{r}_{nk} \mathbf{r}_{kn} + \mathbf{r}_{kn} \mathbf{r}_{nk}}{E_k^{(0)} - E_n^{(0)}}$$

Response of Insulator to static Electric Field



$$\rho_{n'n}^{(1)}(\vec{k}) = ieE \; \frac{f_{n',\vec{k}} - f_{n,\vec{k}}}{(E_{n',\vec{k}} - E_{n,\vec{k}})^2} \; \langle \Psi_{n',\vec{k}} | \frac{\partial H}{\partial k_x} | \Psi_{n,\vec{k}} \rangle \label{eq:rhonormal_problem}$$

Atomic Model of Current-Induced Torques



R^{2w} signal has both planar Hall and anomalous Hall components

SOTs explained to within factor of a few by massive Dirac surface state model

Bulk of the TI - and bulk of any magnetic insulator - can play a role